

Variable Types

Experimental variables:

- 1 **Independent:** Variable that is not changed by the other variables (e.g. age).
- 2 **Dependent:** Measured variable that is affected by others (e.g. cancer risk).

Data types:

- 1 **Nominal / Categorical:** Discrete data that cannot be ordered (e.g. people).
- 2 **Ordinal:** Quantities with a natural order (e.g. Likert scale).
- 3 **Interval:** Ordinal + the interval between each value is equal (e.g. Fahrenheit).
- 4 **Ratio:** Interval + a natural zero point (e.g. elevation).

Multivariate table

Attitude towards uranium mining by age and gender (hypothetical data)

Attitude towards uranium mining	Number of respondents												
	<25		25-34		35-44		45-54		55+		Total		
	F	M	F	M	F	M	F	M	F	M	F	M	T
Strongly favourable	0	0	1	1	3	1	5	2	3	-	12	4	16
Favourable	0	0	1	2	3	2	3	1	0	0	7	5	12
Uncertain	0	0	0	0	1	1	2	2	0	0	3	3	6
Unfavourable	1	1	4	3	1	0	0	0	0	0	6	4	10
Strongly unfavourable	4	8	17	7	8	7	2	3	0	0	31	25	56
Total	5	9	23	13	16	11	12	8	3	0	59	41	100

Figure: Table 16.4 from the book.

2D Chart Anatomy

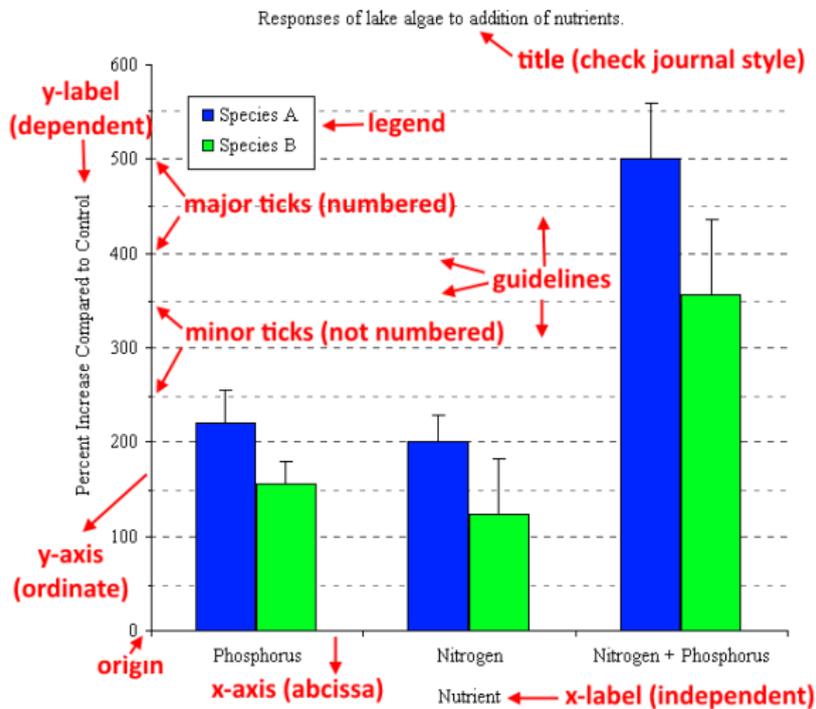


Figure 3. Responses of lake algae to addition of nutrients. Error bars are 95% confidence limits.

N = 50 lakes.

caption

2D Chart Anatomy - Axis Offset

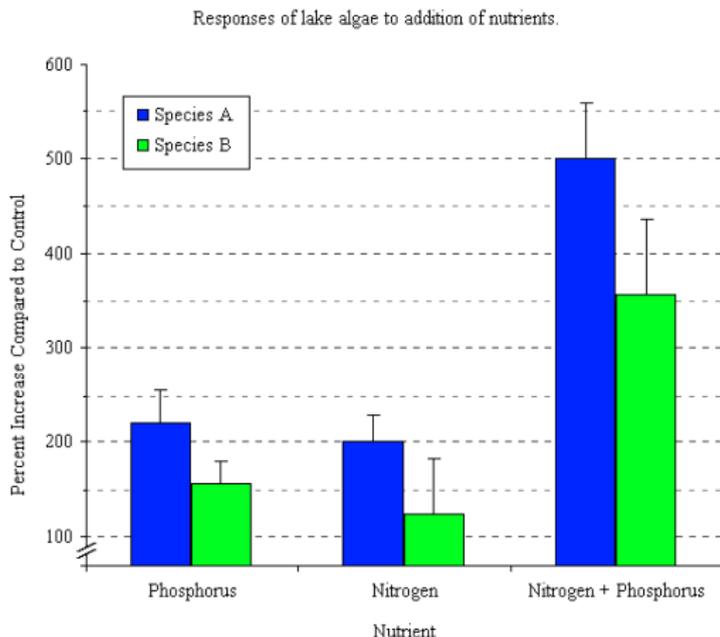


Figure 3. Responses of lake algae to addition of nutrients. Error bars are 95% confidence limits.

N = 50 lakes.

2D Chart Anatomy - Axis Offset

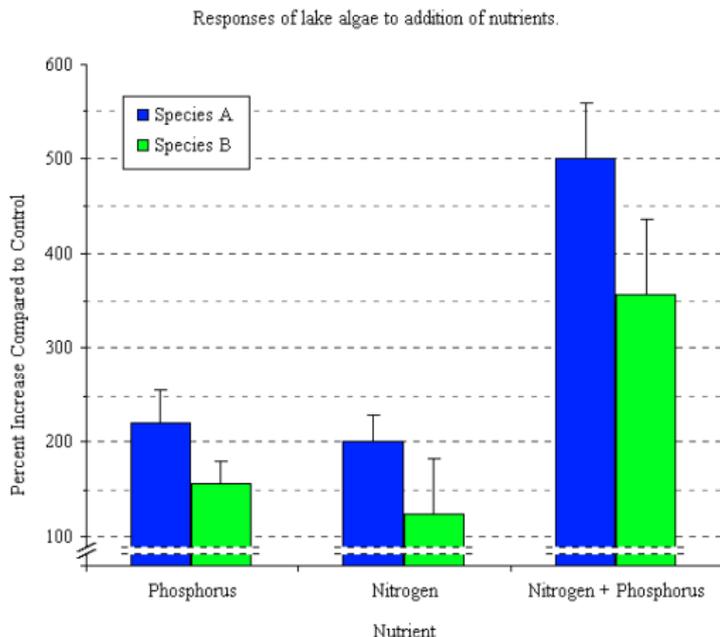
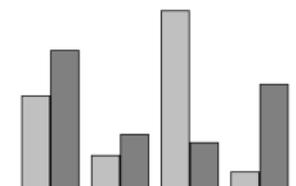
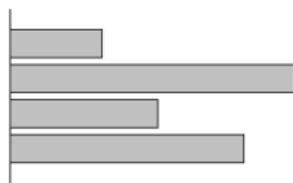
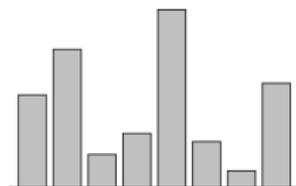


Figure 3. Responses of lake algae to addition of nutrients. Error bars are 95% confidence limits.

N = 50 lakes.

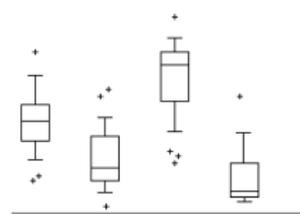
Bar charts

- Use when you want to compare how values of 1 or 2 discrete independent variables affect a numeric dependent variable or count.
- Actual numbers and/or error bars can be added on top of the bars.
- For ordinal data, a histogram may also be used.
- With 2 independent variables, a stacked bar chart can also be used, but this is not recommended for comparisons.



Box plots

- Box plots are like bar charts with extra information.
- They generally show the 1st, 2nd and 3rd quartile of the data, the range and outliers.



Stem-and-leaf display

A stem-and-leaf display let's you show fairly detailed distribution information in the shape of a histogram.

Example (Data)

37, 33, 33, 32, 29, 28, 28, 23,
 22, 22, 22, 21, 21, 21, 20, 20,
 19, 19, 18, 18, 18, 18, 16, 15,
 14, 14, 14, 12, 12, 9, 6

Example from [Lane @ OnlineStatBook](#).

Example (S&L display 1)

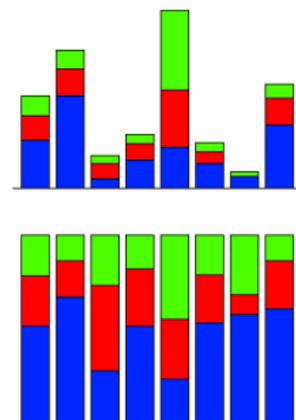
```
3|2337
2|001112223889
1|2244456888899
0|69
```

Example (S&L display 2)

```
3|7
3|233
2|889
2|001112223
1|56888899
1|22444
0|69
```


Stacked bar charts

- Use to show the composition of a thing varying along some discrete dimension.
- Use a 100% bar chart if the absolute value doesn't matter.



Color

Journal

Always check the style of the journal!

Legibility

Keep everything legible!

Account for B&W

Even if you use color, make sure your figures are interpretable if someone prints them without or is color blind. (Don't refer to the color in the text.)

Bar chart color

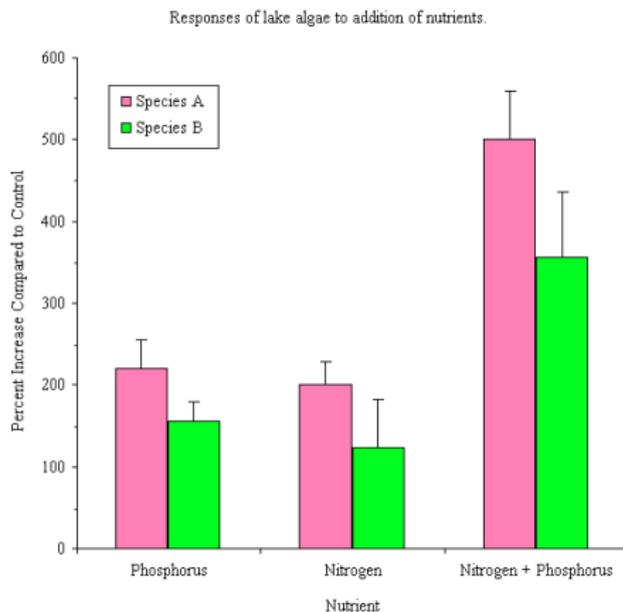


Figure 3. Responses of lake algae to addition of nutrients. Error bars are 95% confidence limits.

N = 50 lakes.

Bar chart color

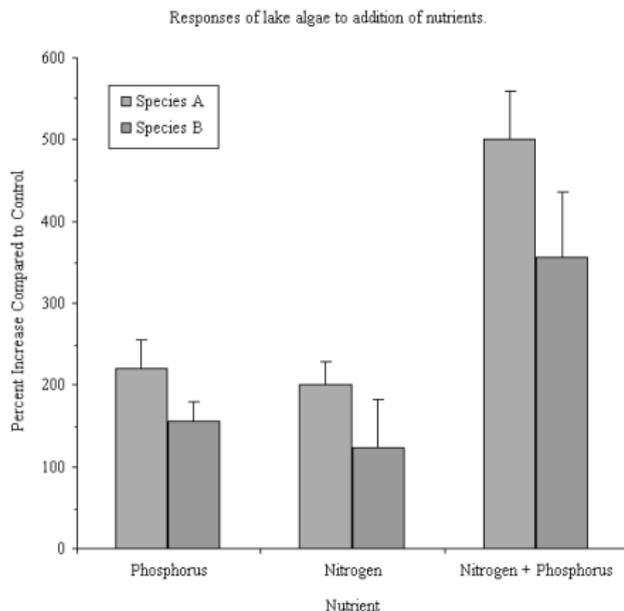


Figure 3. Responses of lake algae to addition of nutrients. Error bars are 95% confidence limits.

N = 50 lakes.

Bar chart color - Hatching

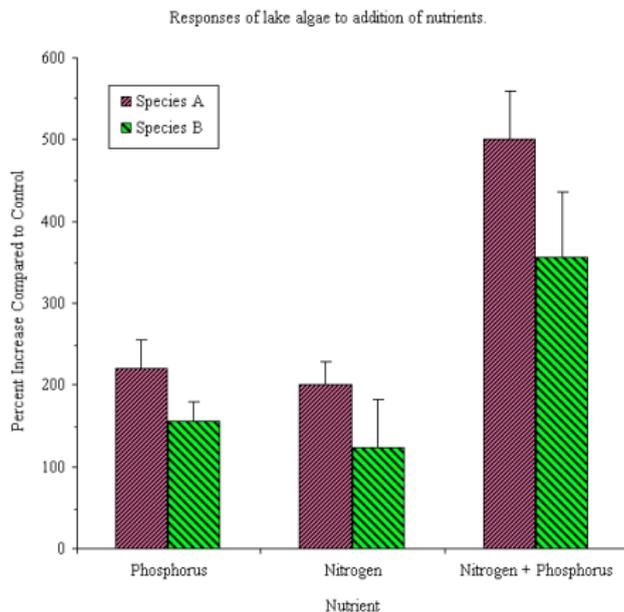


Figure 3. Responses of lake algae to addition of nutrients. Error bars are 95% confidence limits.

N = 50 lakes.

Bar chart color - Hatching

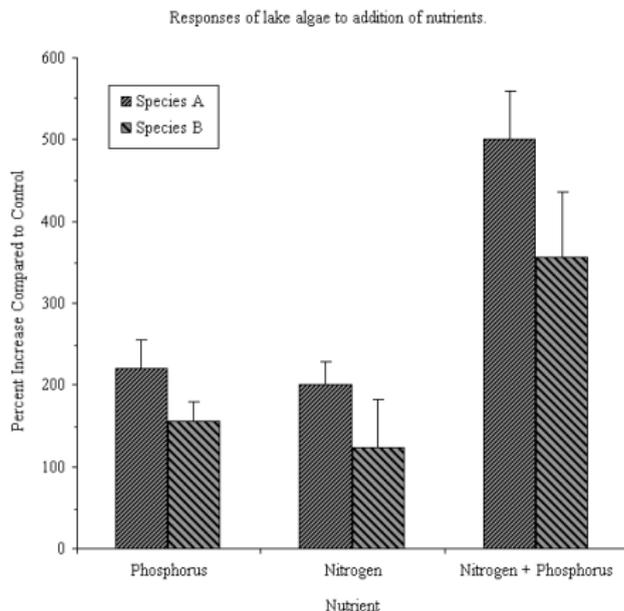


Figure 3. Responses of lake algae to addition of nutrients. Error bars are 95% confidence limits.

N = 50 lakes.

Line chart color - Notches and Line Types

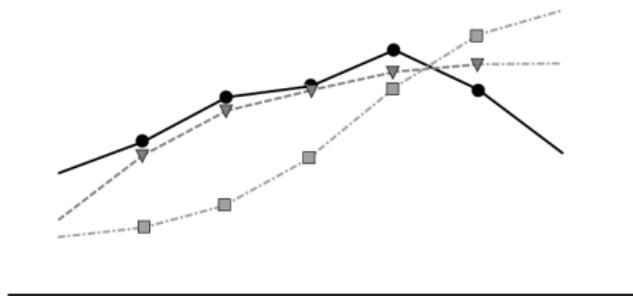


Figure: Use different notches and line types.

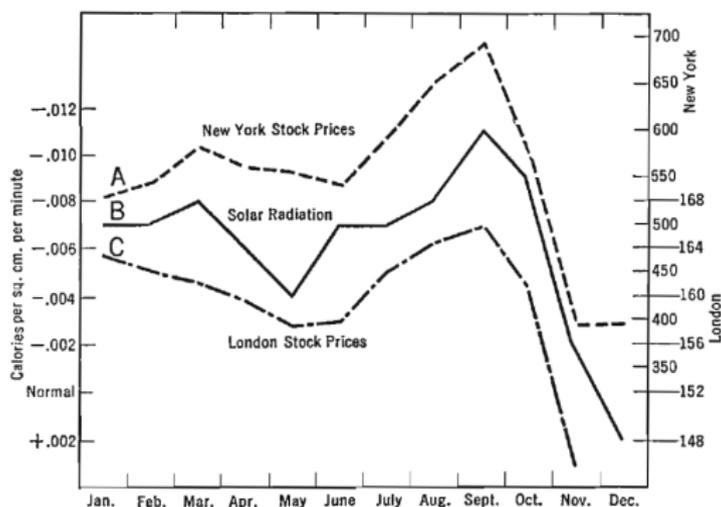
Anscombe

I		II		III		IV	
X	Y	X	Y	X	Y	X	Y
10.0	8.04	10.0	9.14	10.0	7.46	8.0	6.58
8.0	6.95	8.0	8.14	8.0	6.77	8.0	5.76
13.0	7.58	13.0	8.74	13.0	12.74	8.0	7.71
9.0	8.81	9.0	8.77	9.0	7.11	8.0	8.84
11.0	8.33	11.0	9.26	11.0	7.81	8.0	8.47
14.0	9.96	14.0	8.10	14.0	8.84	8.0	7.04
6.0	7.24	6.0	6.13	6.0	6.08	8.0	5.25
4.0	4.26	4.0	3.10	4.0	5.39	19.0	12.50
12.0	10.84	12.0	9.13	12.0	8.15	8.0	5.56
7.0	4.82	7.0	7.26	7.0	6.42	8.0	7.91
5.0	5.68	5.0	4.74	5.0	5.73	8.0	6.89

$N = 11$
 mean of X's = 9.0
 mean of Y's = 7.5
 equation of regression line: $Y = 3 + 0.5X$
 standard error of estimate of slope = 0.118
 $t = 4.24$
 sum of squares $X - \bar{X} = 110.0$
 regression sum of squares = 27.50
 residual sum of squares of Y = 13.75
 correlation coefficient = .82
 $r^2 = .67$

Figure: From Anscombe (1973), "Graphs in Statistical Analysis" via VDQI (page 13)

Multiple Y-Scales



SOLAR RADIATION AND STOCK PRICES

A. New York stock prices (Barron's average). B. Solar Radiation, inverted, and C. London stock prices, all by months, 1929 (after Garcia-Mata and Shaffner).

Figure: From Dewey & Dakin (1947), "Cycles: The science of prediction", p. 144 via VDQI (page 15)

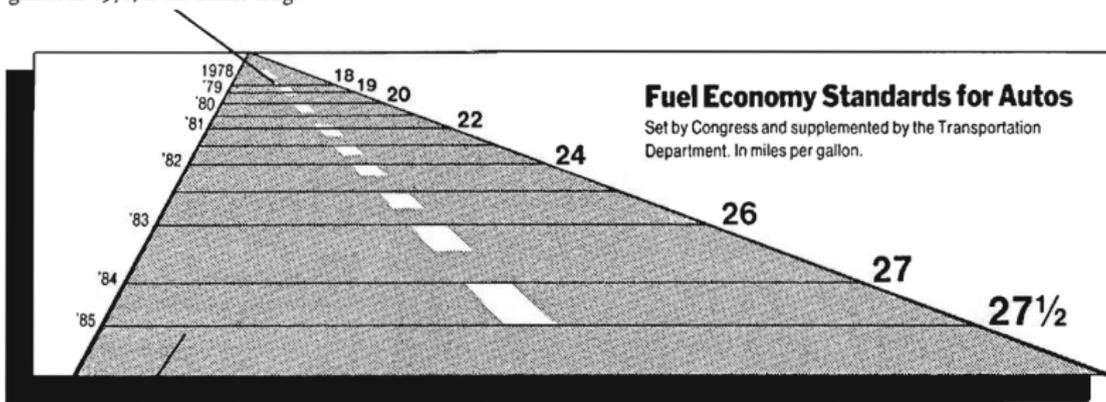
Lie Factor

$$\text{Lie Factor} = \frac{\text{size of effect shown in graphic}}{\text{size of effect in data}}$$

Acceptable between .95 and 1.05.

Exercise

This line, representing 18 miles per gallon in 1978, is 0.6 inches long.



This line, representing 27.5 miles per gallon in 1985, is 5.3 inches long.

Figure: From New York Times, August 9 1978, p. D-2 via VDQI (page 57) Lie factor: 14.8 or 111

Design and Data Variation

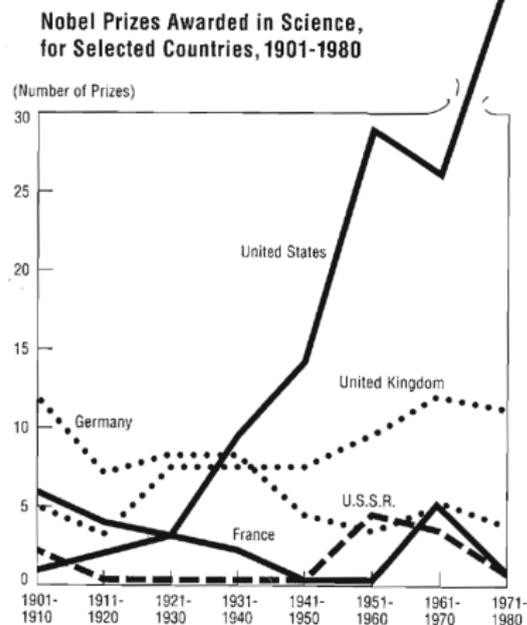
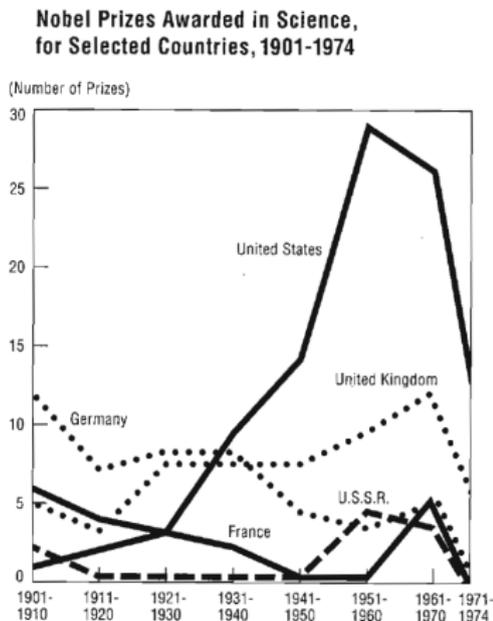


Figure: From National Science Foundation, Science Indicators, 1976 (Washington D.C., 1976) via VDQI (page 60)

Money

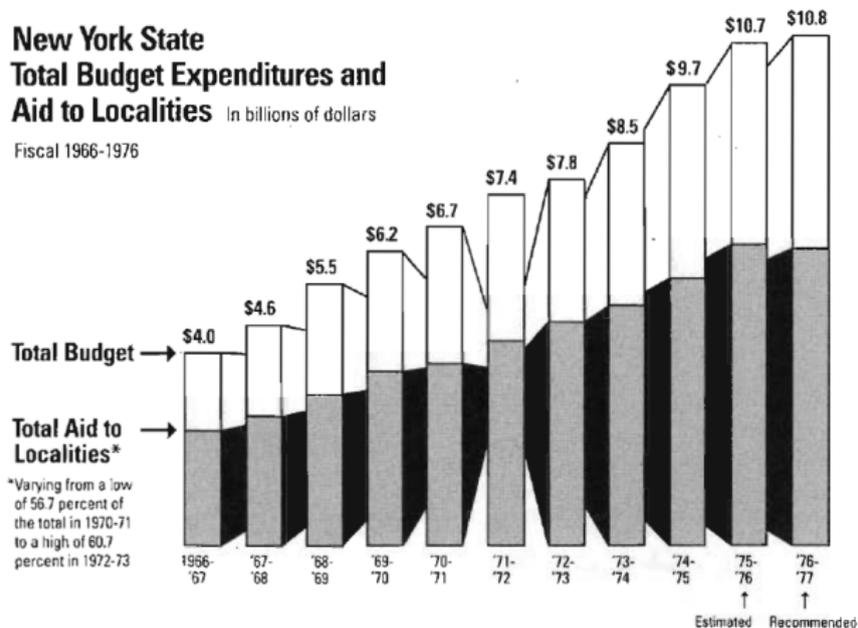


Figure: From New York Times, February 1 1976, p. IV-6 via VDQI (page 66)

Correct for inflation and other factors

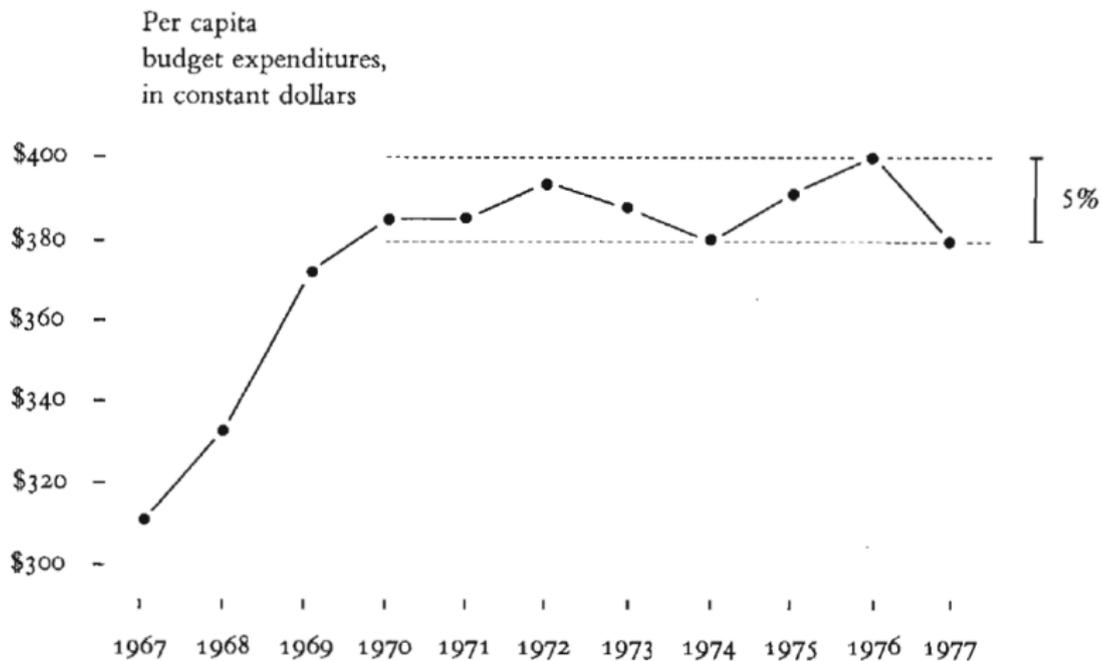


Figure: From VDQI (page 68)

Context



Figure: From Campbell & Ross (1970), "The Connecticut Crackdown on Speeding: Time Series Data in Quasi-Experimental Analysis" via VDQI (page 74)

Context

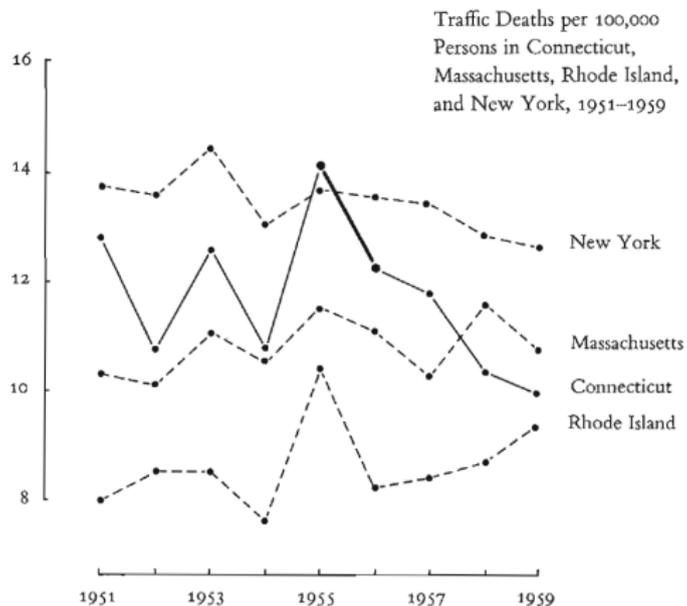


Figure: From Campbell & Ross (1970), "The Connecticut Crackdown on Speeding: Time Series Data in Quasi-Experimental Analysis" via VDQI (page 75)

Numbers have order and magnitude

Comparative Annual Cost per Capita for care of Insane in Pittsburgh City Homes and Pennsylvania State Hospitals.

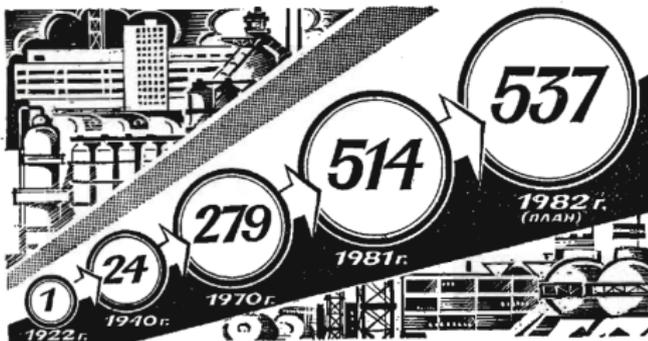


Figure: From Pittsburgh Civic Commission (1911), "Report on Expenditures of the Department of Charities" and Pravda, May 24 1982 p.2 via VDQI (page 55 and 76)

Truncated Y-Axis

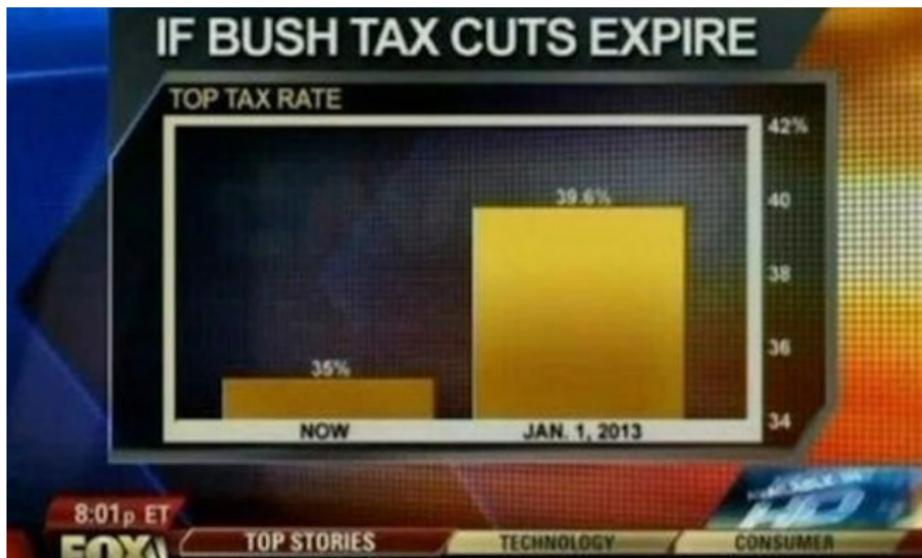


Figure: Via [Parikh @ Gizmodo](#).

Different Y-Axis

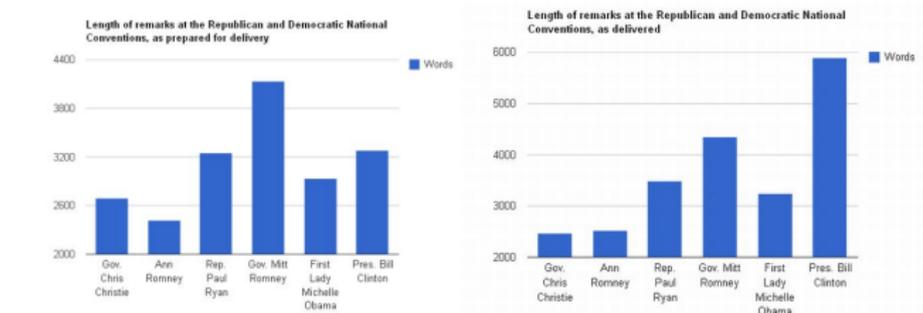


Figure: From [Cliff @ Washington Post](#).

Poorly used cumulative graph

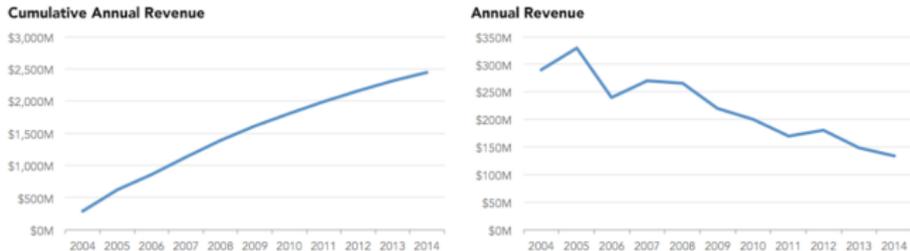


Figure: From [Parikh @ Gizmodo](#).

Data-Ink

Data-ink

Data-ink is the non-erasable core of a graphic; the non-redundant ink arranged in response to variation in the numbers presented.

Data-Ink Ratio

$$\begin{aligned} \text{Data-ink ratio} &= \frac{\text{data-ink}}{\text{total ink used to print the graphic}} \\ &= \text{proportion of a graphic's ink devoted} \\ &\quad \text{to the non-redundant display of data-information} \\ &= 1.0 - \text{proportion of a graphic that can be erased} \\ &\quad \text{without loss of data-information.} \end{aligned}$$

Examples

Data-Ink

- Lines in a line graph, bars in a bar graph, dots in a scatter plot, etc.
- Labels
- Data values

Non-Data-Ink

- Axes
- Ticks
- Grid lines
- Decorations

Maximize Data-Ink-Ratio

- Depict more data
- Erase non-data-ink
- Erase redundant data-ink

Within reason!

Exercise

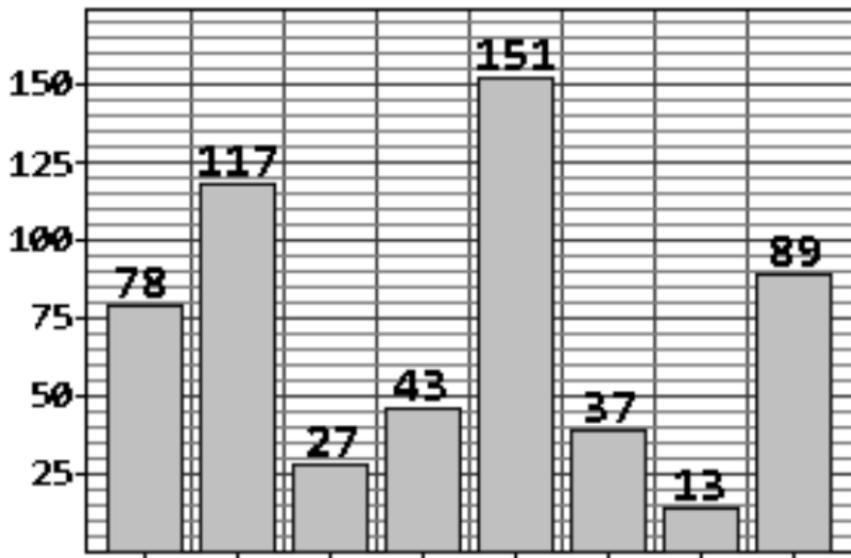


Figure: See VDQI (page 96 and 126-128)

How can we increase the data-ink-ratio?

Exercise 2

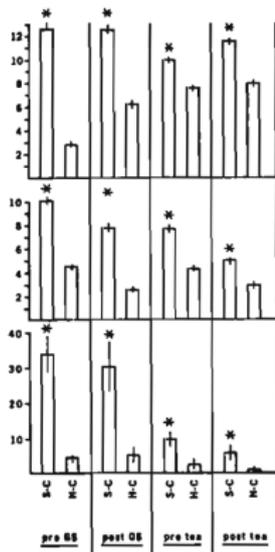


Figure: From Kuznicki & McCutcheon (1979) via VDQI (page 100)

Exercise 2

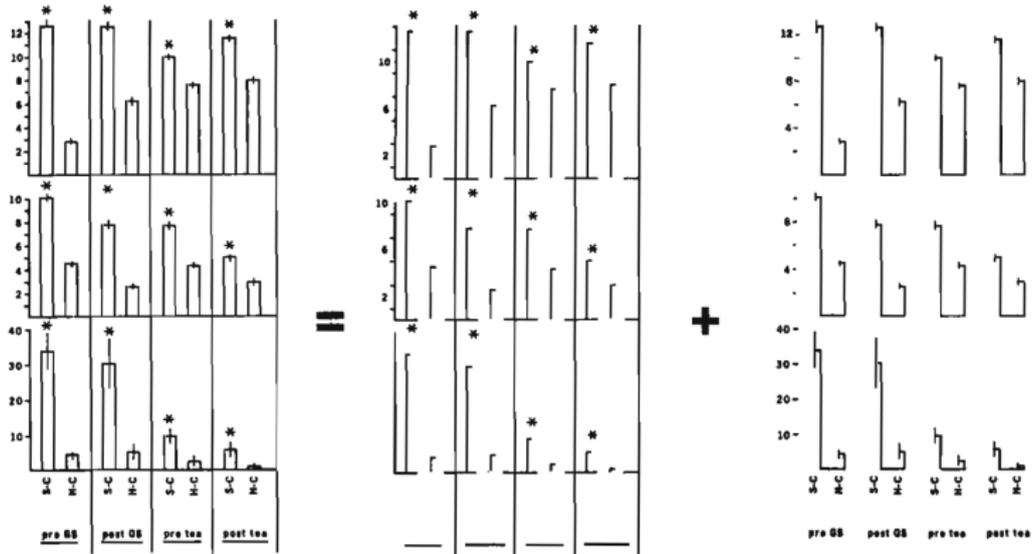


Figure: From VDQI (page 102)

Boxplots

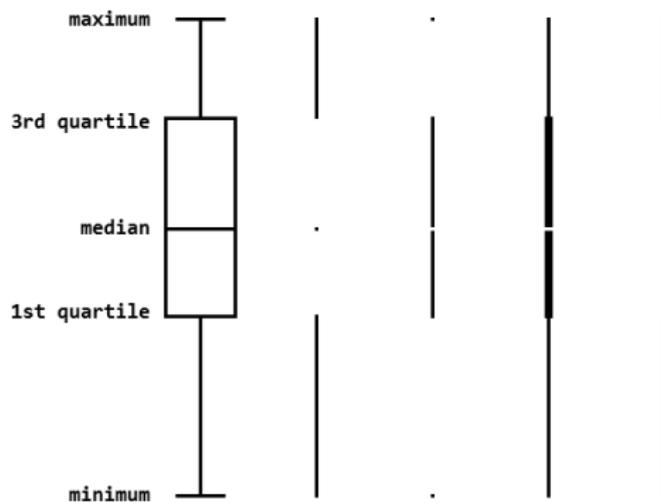


Figure: After VDQI (page 123-125)

Range-Frame



Figure: From VDQI (page 132)

Range-Frame

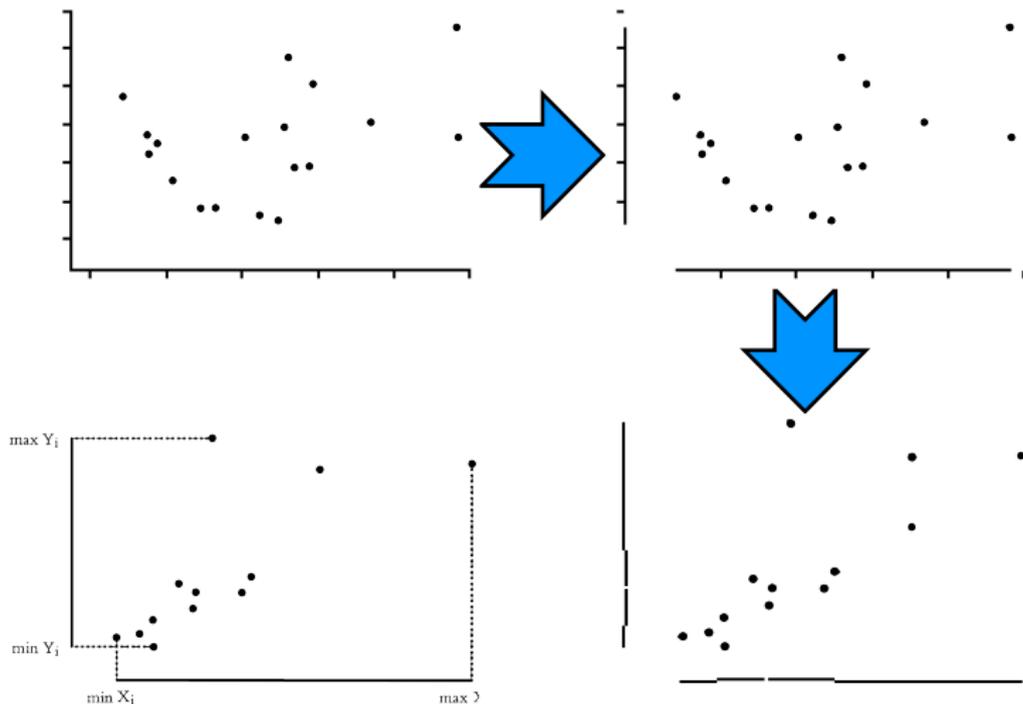


Figure: From VDQI (page 130-132)

Distribution on axes

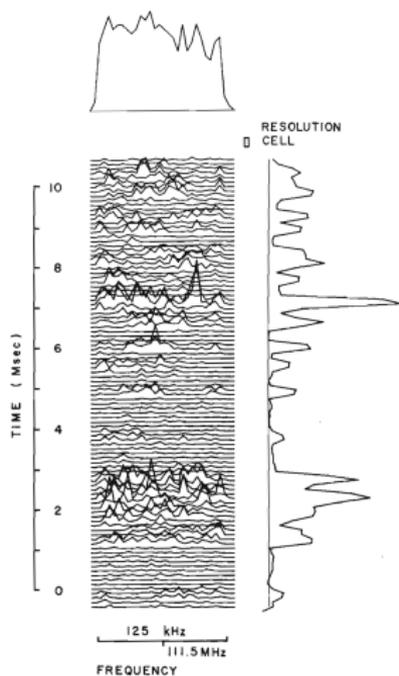


Figure: From Hawkins & Rickett (1975), "Pulsar Signal Processing", p. 108 via VDQI (page 134)

Data Density

$$\text{data density of a graphic} = \frac{\text{number of entries in data matrix}}{\text{area of data graphic}}$$

Maximize Data Density

- Depict more data
- Shrink the graphic
- Use multifunctioning graphical elements

Within reason!

Stem-and-leaf display

A stem-and-leaf display let's you show fairly detailed distribution information in the shape of a histogram.

Example (Data)

37, 33, 33, 32, 29, 28, 28, 23,
22, 22, 22, 21, 21, 21, 20, 20,
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14, 14, 14, 12, 12, 9, 6

Example from [Lane @ OnlineStatBook](#).

Example (S&L display 1)

```
3|2337
2|001112223889
1|2244456888899
0|69
```

Example (S&L display 2)

```
3|7
3|233
2|889
2|001112223
1|56888899
1|22444
0|69
```

Number Plots

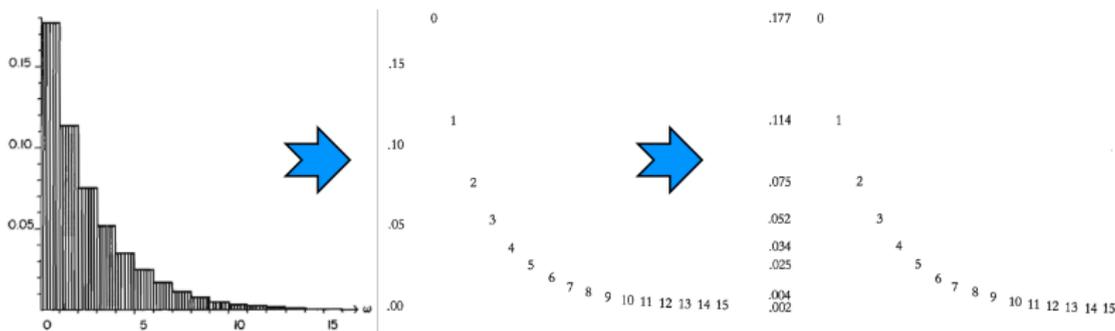


Figure: From stylesheet of the Journal of the American Statistical Association (left) and VDQI (page 150-151)

Chernoff Faces



Figure: From Wainer & Thissen (1981), "Graphical Data Analysis" via VDQI (page 142)

See also Chernoff (1973), "The Use of Faces to Represent Points in k-Dimensional Space Graphically" and [Wikipedia](#).