

# Planning in the “Real World”

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## Why does STRIPS not suffice?

- Time impacts planning and especially concurrent plans
- Resources are difficult to handle in STRIPS
  - Unary resources, such as equipment (can be done)
  - Multiple resources, such as equipment (hard, but not impossible)
  - Numerical resources, such as fuel (very hard and expensive)
  - etc.
- Numerical calculations are impossible in STRIPS
- Complex conditions and state constraints are very hard in STRIPS
- Uncertainty and sensing is very hard to do in STRIP

But, can still use strips in real world, if we are clever...

# Planning with Time and Resources

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## Planning techniques for complex domains

- Hierarchical Task Networks
- Constraint-based Planning

## Planning techniques for uncertainty/sensing

- Conformant planning
- Conditional planning
- Execution and replanning
- Continuous planning

# Hierarchical Task Networks

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## Basic Idea:

- Describe higher-level action as a set of lower-level actions
- Example: BuildHouse has actions:
  - Put in foundation
  - Put up walls
  - Add roof
  - Add interiors
  - Do exteriors
- along with conditions about the actions:
  - Foundation must come before walls
  - Roof comes before interiors
  - Adding roof requires resources “roofers”, “crane”, “access”,...
  - etc.

## Search technique:

- Select expansion for high-level action and resolve conditions
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# Hierarchical Task Networks

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## Advantages of HTN

- Can describe more complex conditions than in STRIPS
- Can utilize structure to separate subgoals

## Disadvantages of HTN

- Requires specifying “how to” in planning domain
- Expensive to add completely new goals (e.g., build a rowhouse)

## More realistic approach

- Mix HTN and STRIPS to permit both hierarchical breakdown and actions that have preconditions and effects.

# Constraint-based Planning

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## Basic Idea:

- Describe each action, state, timepoint, resource allocation, etc., with variables
- Specify relations, timing, resources, etc. as constraints on variables
- When new actions are added, add new variables and constraints
- Use inferences to maintain consistency and identify complete plans
- Search: Select underspecified variable and make decisions

# Planning with Uncertainty

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## Example:

- Rover is to take a picture but not sure about exact location

## Conformant planning

- Take pictures in all directions and from all possible locations

## Conditional planning

- Senses location and then either drive or take picture

## Execution and replanning

- Drive and take picture, but track outcome and replan if needed

## Continuous planning

- Drive and take picture, but continuously look for better plans, e.g., also grab sample that was to be done later

# So what can we do with STRIPS in real world?

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## Rover domain (almost “real world”)

- Actions:
  - Move to location
  - Pick up object
  - Drop object
  - ...
- Sensor information:
  - Outcome of actions
  - Location
  - ...

But STRIPS cannot handle sensing, execution, etc.

- However, can use STRIPS as part of that

# So what can we do with STRIPS in real world?

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## Interleave planning and step execution

- Use sensing to determine current state
- Consider goals to be achieved next
- If current plan still works, continue with that
- Else, build plan to achieve goals from current state
- Execute one or more steps in plans
- Repeat

## Possible implementation

- Core planner is simple STRIPS
- Domain must be specified
- Execution understands plans and executes them stepwise



# Decisions under Uncertainty

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## Probability and inference

- Uncertainty and decisions
- Axioms of probability
- Probability tables and Bayes-nets

## Decisions under uncertainty and adversity

- Markov decision problems
- Methods to solve Markov decision problems
- Game theory

# Why worry about uncertainty?

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Uncertainty is not randomness

- Probabilities impacted by decisions

Uncertainty may be in knowledge, not reality

- Information not available or not measurable

Can do better by considering uncertainty

- Likeliest outcome not necessary best
- Can impact uncertainty (e.g., by sensing or behavior)

Use probability theory to work with uncertainty

Use utility theory to maximize value overall

- Utility is sum over probability of result  $\times$  value of result

# Basic notions in probability theory

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## Random variables

- Variables taking on values according to probabilities

## Probability distribution

Weather	Probability
sun	0.3
rain	0.5
snow	0.25

## Joint probability distribution

Weather	Grass=dry	Grass=wet	Grass=frozen
sun	0.2	0.05	0.05
rain	0.05	0.4	0.05
snow	0.02	0.08	0.15

# Conditional and unconditional probabilities

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## Unconditional probability

- Example:  $P(\text{weather}=\text{rain}) = 0.5$

## Conditional probability

- Example:  $P(\text{weather}=\text{rain} \mid \text{grass}=\text{wet}) = 0.9$

# Probability Axioms

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## Axioms

- $0 \leq P(a) \leq 1$
- $P(T) = 1$
- $P(F) = 0$
- $P(a \vee b) = P(a) + P(b) - P(a \wedge b)$

## Conditional probability axioms

- $P(a|b) = P(a \wedge b) / P(b)$
- $P(a \wedge b) = P(a|b) P(b)$

# Probability calculations

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Let's calculate:

- $P(\text{Weather}=\text{rain})$
- $P(\text{Weather}=\text{rain} \mid \text{Grass}=\text{wet})$

Weather	Grass=dry	Grass=wet	Grass=frozen
sun	0.2	0.05	0.05
rain	0.05	0.4	0.05
snow	0.02	0.08	0.15

# Independent variables

If variables a og b eru independent:

- $P(a \wedge b) = P(a) P(b)$

Example:

- Stocks is independent of Weather and Grass

	Stocks=up Grass=dry	Stocks=up Grass=wet	Stocks=up Grass=frozen	Stocks=down Grass=dry	Stocks=down Grass=wet	Stocks=down Grass=frozen
Weather						
sun	0.1	0.025	0.025	0.1	0.025	0.025
rain	0.025	0.2	0.025	0.025	0.2	0.025
snow	0.01	0.04	0.075	0.01	0.04	0.075

Result:

- Can make two smaller tables

Weather	Grass=dry	Grass=wet	Grass=frozen
sun	0.2	0.05	0.05
rain	0.05	0.4	0.05
snow	0.02	0.08	0.15

Stocks	
up	0.5
down	0.5

# Bays Rule

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## Bays Rule:

- $P(b|a) = (P(a|b) P(b) / P(a))$

## Use:

- Often we know relation in one direction, but not other
- Example: 80% of people with flue have fever
- Want to know: If person has fever, what are odds of having flue
- Let's say odds of fever are 2% overall and odds of flue 0.1%
- Then, odds of patient having flue, given fever, is:  
 $(0.8 * 0.001) / 0.02 = 0.04 = 4\%$



# Conditional independence

## Basic idea:

- Independent variables are good™
- But, most variables end up being dependent
- However, many are dependent “through another variable

## Example:

Weather	Grass=dry	Grass=wet	Grass=frozen
sun	0.2	0.05	0.05
rain	0.05	0.4	0.05
snow	0.02	0.08	0.15

Weather	BBQ=yes	BBQ=no
sun	0.7	0.3
rain	0.05	0.95
snow	0.01	0.99

# Conditional Independence

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## Skilgreining:

- Breytur  $a$  og  $b$  eru óháðar ef gildi  $C$  er gefið, ef
$$P(a \wedge b \mid C=c) = P(a \mid C=c) P(b \mid C=c)$$

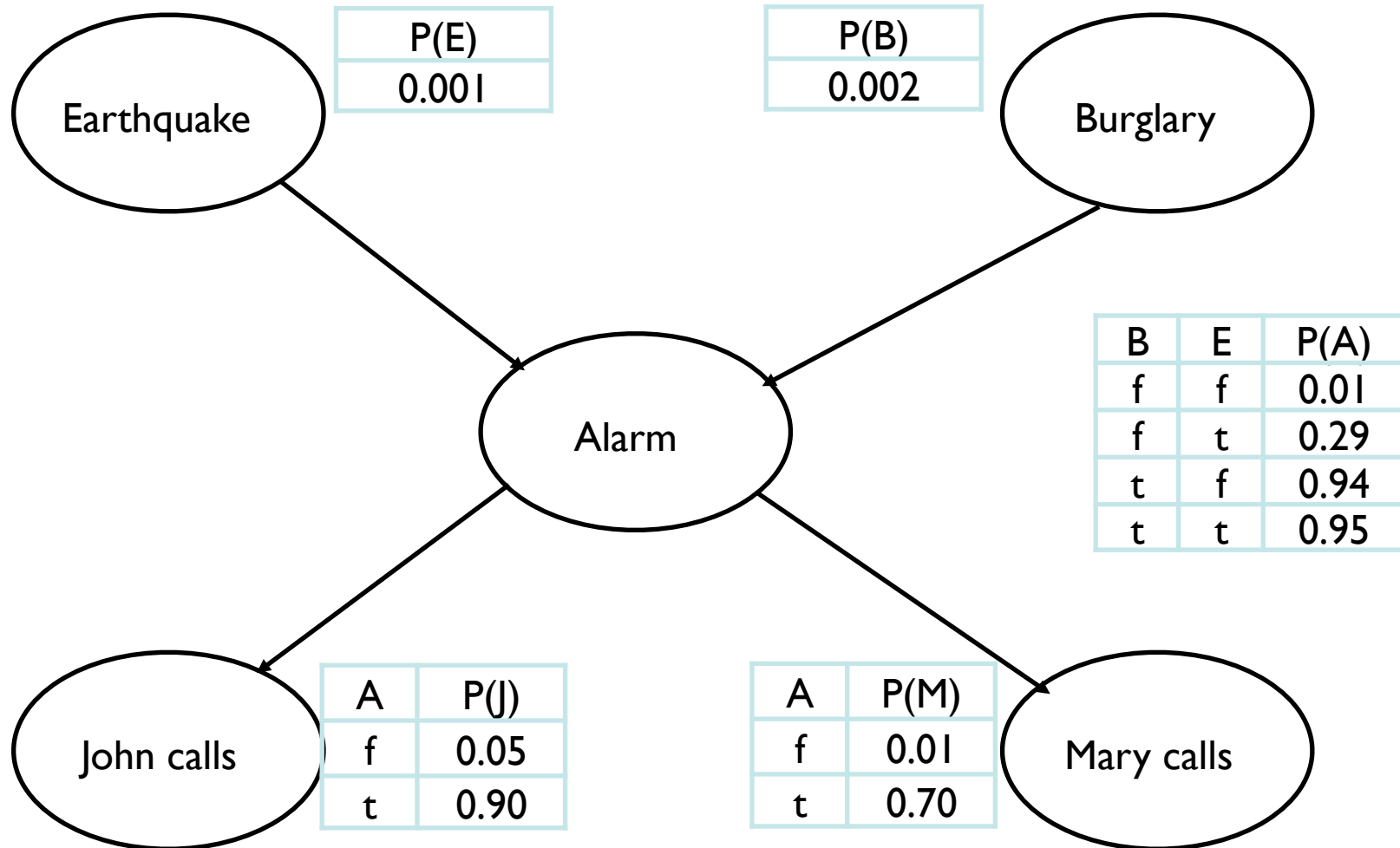
## Notkun með Bays reglu:

- $P(\text{Weather}=\text{rain} \mid \text{Grass}=\text{wet} \wedge \text{BBQ}=\text{no})$   
 $= \alpha P(\text{Grass}=\text{wet} \mid \text{Weather}=\text{rain}) P(\text{BBQ}=\text{no} \mid \text{Weather}=\text{rain})$

## Nytsemi:

- Getum notað Bays net til að lýsa líkindum og venslum líkinda á þjappaðan hátt
- Það gerir okkur kleyft að draga ályktanir út frá líkindaupplýsingum

# Example of Bays net



# Planning in uncertain World

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## Problem

- How to decide what to do when outcomes are uncertain, but still do the right thing at each point

## Basic idea

- Build a policy that says what to do in each possible position

## Markov Decision Problems

- Probability of outcomes, given a state and an action
- Probability independent of earlier states and actions

## Game Theory

- Possible states and outcomes, own actions and adversary actions

# Markov ákvörðunarvandamál

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## Færslur í óvissu

- Fyrir hverja stöðu og hverja aðgerð, fáum líkindadreifingu á hvaða stöðu við lendum í

## Markov færslur (Markov transitions)

- Færslur þar sem líkindi á niðurstöðu færslu eru einungis háð stöðu og aðgerð, en ekki fyrri stöðum og aðgerðum

## Markov ákvörðunarvandamál

- Upphafsstaða  $s_0$
- Færslulíkan  $T(s, a, t) = p$ 
  - Fyrir hverja stöðu og hverja aðgerð, fáum líkindadreifingu fyrir stöður sem við getum lent í - ef  $a$  er framkvæmt í stöðu  $s$ , lendum í með líkindum  $p$
- Ávinningsfall  $R(s)$ 
  - Fyrir hverja stöðu, fáum ávinning af því að vera í þeirri stöðu

# Lausnaraðferðir

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## Markmið

- Ákvarða fyrir hverja stöðu hvað sé best að gera
- Ef við vitum gildi hvernar stöðu er auðvelt að ákveða aðgerðir  
- veljum þá aðgerð sem gefur hæsta viðbúna gildi (expected value)

## Gildisítrun (value iteration)

- Reiknum út gildi hvernar stöðu, miðað við að fylgjum stefnu sem leitast við að fara í stöður með hærri gildi
- Raunverulegt gildi stöðu, miðað við samsavarandi stefnu er  
$$U_{\pi}(s) = E \left[ \sum \gamma^t R(s_t) \mid \pi \right]$$
- En getum notað auðveldari jöfnu sem lýsir venslum staða í lausn

## Stefnuítrun (policy iteration)

# Uppfærsla stöðugilda

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Bellman jafnan

- $U(s) = R(s) + \gamma \max_a \sum_t T(s,a,t) U'(t)$

þar sem

- $U'$  er núverandi gildismat
- $R$  er fall sem gefur ávinning fyrir að vera í stöðu  $s$
- $\gamma$  er hlutfall gildis framtíðarávinnings og fengins ávinnings
  - betri er einn fugl í hendi en tveir í skógi

Notum hana til að uppfæra stöðugildi í ítrun

- $U(s) = R(s) + \gamma \max_a \sum_t T(s,a,t) U'(t)$

# Gildisítrun

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$U(s)=0$  fyrir öll  $s$

Endurtökum

- $U' = U$

- fyrir hverja stöðu  $s$

- $U(s) = R(s) + \gamma \max_a \sum_t T(s,a,t) U'(t)$

þar til nægilegt jafnvægi næst